

Exploring the magnetic Hertzsprung-Russell diagram with spectropolarimetry

Julien Morin

Institut für Astrophysik Göttingen

International School on Astrophysical Polarimetry

Centre Paul Langevin, Aussois, France

5th June 2013

Outline

- 1 Magnetic fields: a crucial ingredient of stellar physics
- 2 Detection and characterization of stellar magnetic fields
- 3 A (likely biased) selection of results
- 4 Summary

Outline

- 1 Magnetic fields: a crucial ingredient of stellar physics
 - Stellar magnetic fields are ubiquitous
 - Stellar magnetic fields play a key role
 - The origin of stellar magnetic fields
- 2 Detection and characterization of stellar magnetic fields
- 3 A (likely biased) selection of results
- 4 Summary

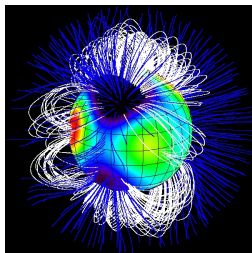
Stellar magnetic fields are ubiquitous

- Measured across H-R diagram

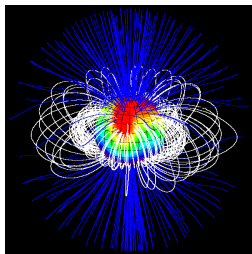
- All masses
- All evolutionary stages

- Wide variety of properties

- Intensity/geometry/variability



τ Sco, 15 $M_{\odot}$ *Donati et al. (2006a)*



V374 Peg, 0.3 $M_{\odot}$ *Donati et al. (2006b)*

Magnetic fields play a key role (1/2)

■ Activity

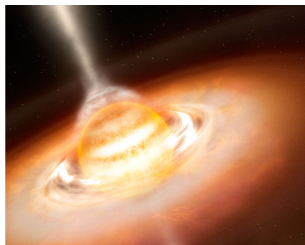
- Observable across electromagnetic spectrum
- Impact of **B** on all atmospheric layers



Credit: F. Espenak

■ Formation

- Phase where **B** has strongest impact
 - Jets launching
 - Magnetospheric accretion

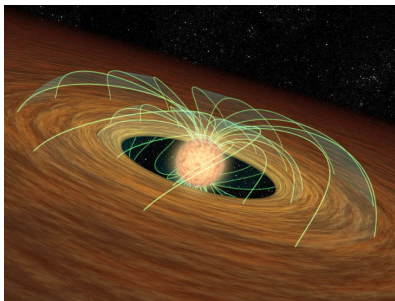


Credit: ESO

Magnetic fields play a key role (2/2)

■ Rotation

- During formation
 - star–disc interaction
 - Post T Tauri
 - Magnetized winds
 - Much more efficient than non-magnetized
- Schatzman (1962)*



Credit: NASA / JPL-Caltech / R. Hurt

■ Star–planet interaction

- Stellar wind
- Coronal mass ejection
- Planetary magnetosphere
- Planetary atmosphere

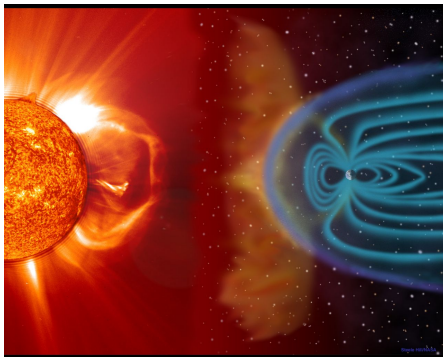
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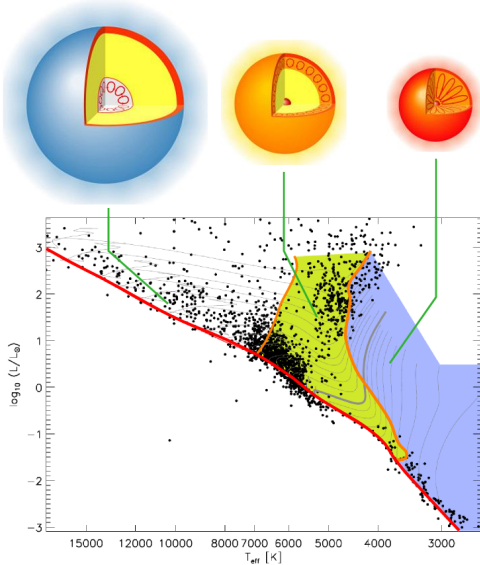
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Credit: NASA / ESA

The origin of stellar magnetic fields (1/2)



Adapted from [Reiners \(2008\)](#)
star sketches credit J. Bennett et al.

High-mass star:
Simple steady field

→ Fossil field ?

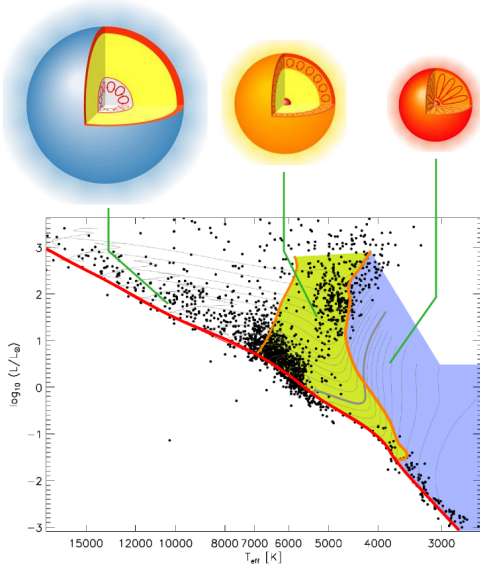
Partly convective star:
Complex **B**
temporal evolutions

→ Solar-type dynamo

Fully convective star:
No tachocline

→ Non-solar dynamo

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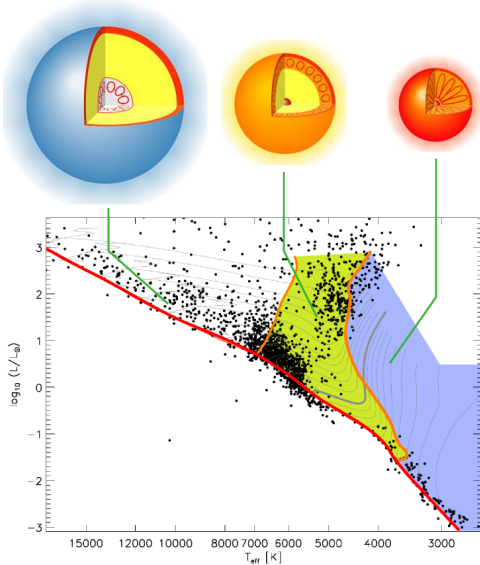
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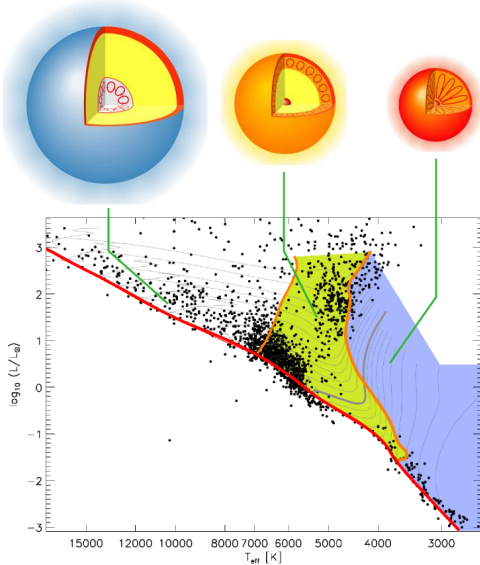
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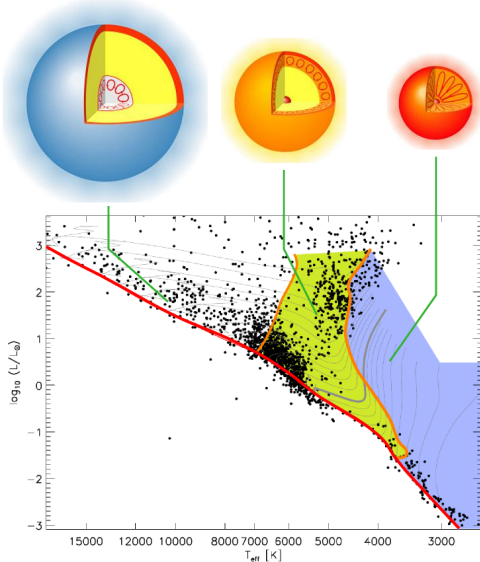
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Relation
★ parameters
↔ **B** properties?

The origin of stellar magnetic fields (2/2)

Dynamo action

■ Amplifies and sustains **B**

- Conversion $E_{\text{kin}} \rightarrow E_{\text{mag}}$
- Induction effect

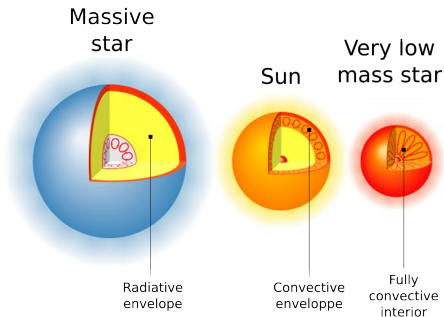
$$\frac{\partial \mathbf{B}}{\partial t} = \underbrace{\nabla \times (\mathbf{u} \times \mathbf{B})}_{\text{induction}} + \underbrace{\eta \Delta \mathbf{B}}_{\text{dissipation}}$$

■ Solar dynamo

- Ω -effect: poloidal $\rightarrow$ toroidal
- Poloidal field regeneration?
- Role of tachocline

■ Stellar magnetic fields

- Different regime of parameters
- Non-solar dynamo



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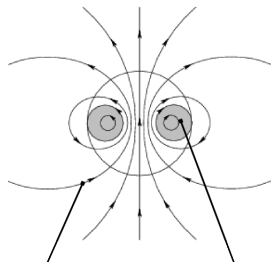
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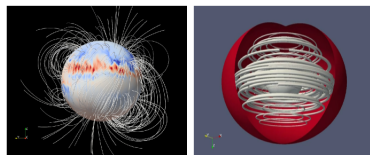
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Poloidal + Toroidal



*Adapted from figures by
J. Braithwaite and T. Gastine*

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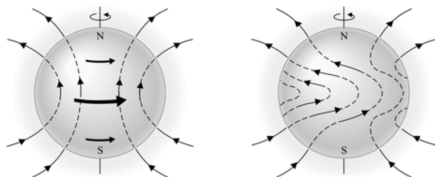
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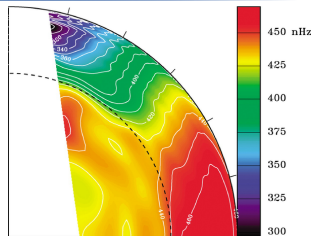
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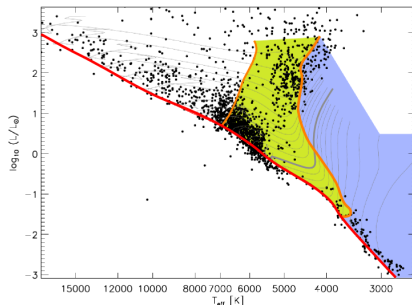
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Internal angular velocity
Shu et al., 2006; from
SOHO-MDI data



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 - Indirect measurements: stellar activity
 - Direct measurements of photospheric magnetic fields
 - Longitudinal/transverse field measurements
 - High-resolution spectropolarimetry
 - Zeeman-Doppler Imaging
- 3 A (likely biased) selection of results
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Indirect measurements: stellar activity

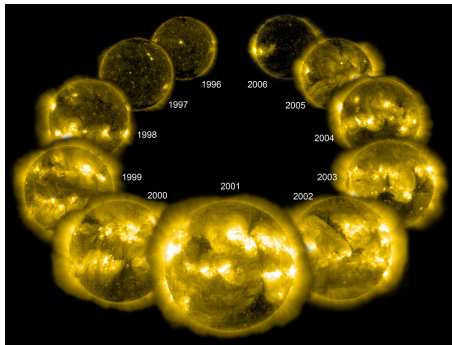
■ Magnetic field

- Photospheric features
 - Visible photometry
 - HR spectroscopy
- Chromosphere
 - UV, vis. emission lines
- Corona
 - X-ray, radio

■ Spatial + temporal correlations

■ Usual proxies for stellar **B**

- CaII H&K emission
- Coronal X-ray emission



SOHO, EUV

Indirect measurements: stellar activity

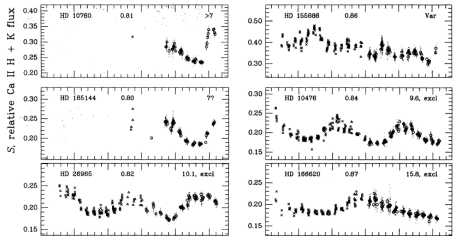
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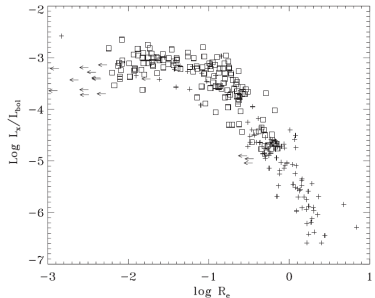
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Baliunas et al. (1995)



Pizzolato et al. (2003)

Direct measurements of photospheric fields

- Direct $\mathbf{B}_{\text{photosph}}$ measurements

- Zeeman effect

- Measure “magnetic flux”: $\langle \|\mathbf{B}\| \rangle$

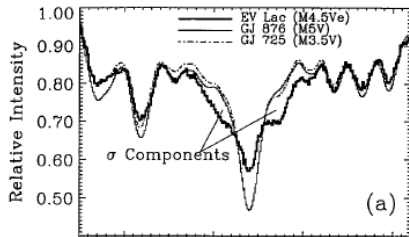
- Atomic lines
- Molecular lines

- Multi-component models

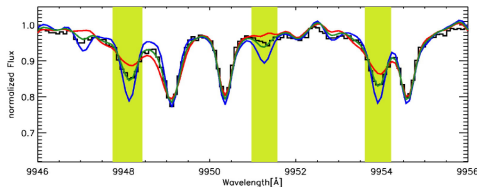
- Weakly sensitive to $\mathbf{B}$ orientation

- Partly degenerate

- Low to moderate $v \sin i$



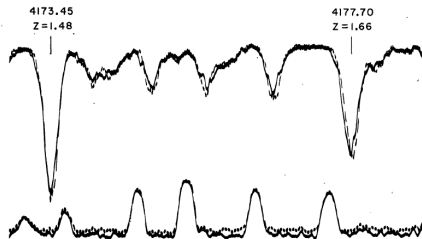
Johns-Krull & Valenti (1996)



GJ 729, FeH Wing-Ford band
Reiners & Basri (2006)

Longitudinal/transverse field measurements

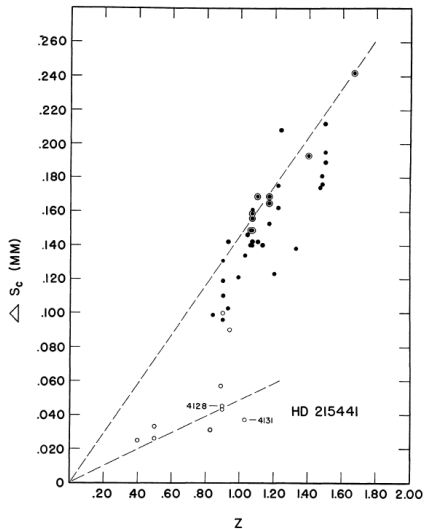
- B_ℓ : longitudinal field
- Zeeman-induced circ. pol.
 - Shift RHCP/LHCP spectra
 - $B_\ell \propto \Delta\lambda_B$
- 1st detection on another star than the Sun: *Babcock (1947)*
- Differential measurement / weakly affected by modelling error
- Requires high S/N ($\sim 10^4$)
- Similarly linear polarisation
→ transverse field
- Limited information:
1st moment of Stokes V



Babcock (1947)

Longitudinal/transverse field measurements

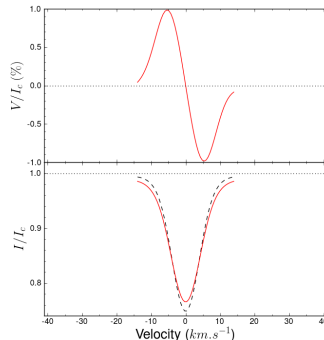
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Babcock (1960)

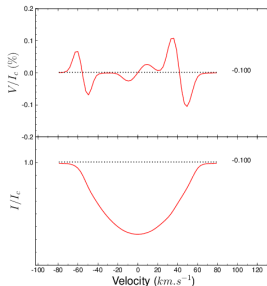
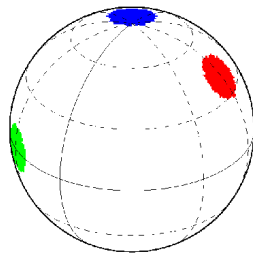
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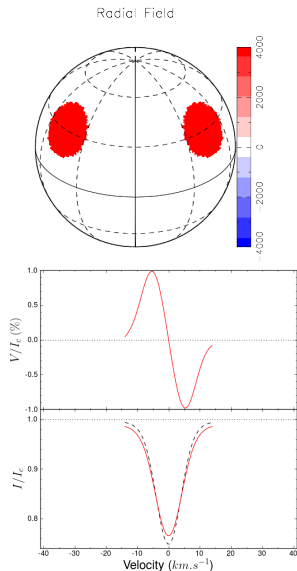
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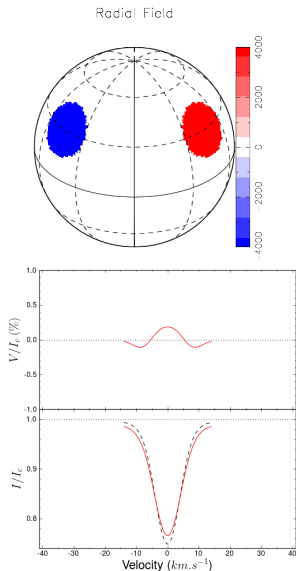
High-resolution spectropolarimetry

- Sensitive to vector properties
- Partial cancellation
 - Blind to small-scale field
- “Weak-field regime”
 - V : typically $10^{-3} - 10^{-2} \times I_c$
 - Q, U : typically $0.1 \times V$
- ➔ Requires $S/N \sim 10^3 - 10^4$
- Multi-line extraction
 - Self-similar signal in all lines
 - Least-Square Deconvolution
Donati et al. (1997)
 - Behaves as real line up to a few kG
Kochukhov et al. (2010)
- Efficient instruments:
CFHT/ESPaDOnS, TBL/NARVAL,
LaSilla3.6m/HARPSpol



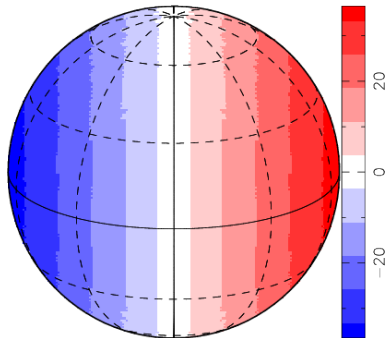
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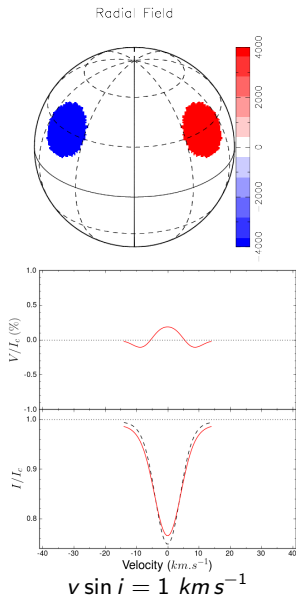
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Equal RV stripes

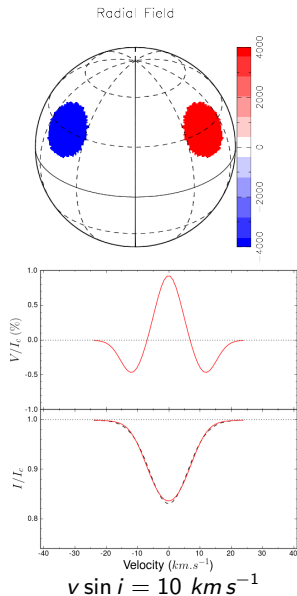
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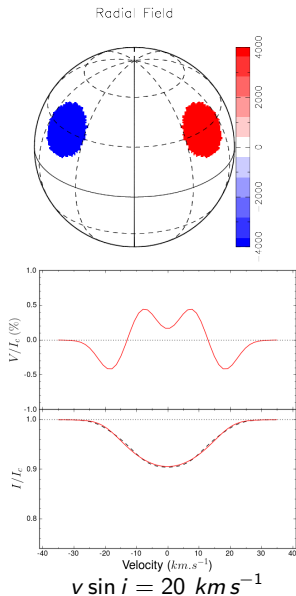
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Zeeman-Doppler Imaging: principles

■ ZDI: principle *Semel (1989)*

- Properties Zeeman effect
- Doppler effect
- Rotational modulation
- ➞ Vector **B**

■ Ambiguity/degeneracy

- Regularization required
 - e.g. maximum entropy
Donati & Brown (1997)

■ Spherical harmonics decomposition *Donati et al. (2006)*

- Solenoidal field
- Limit reconstruction scale
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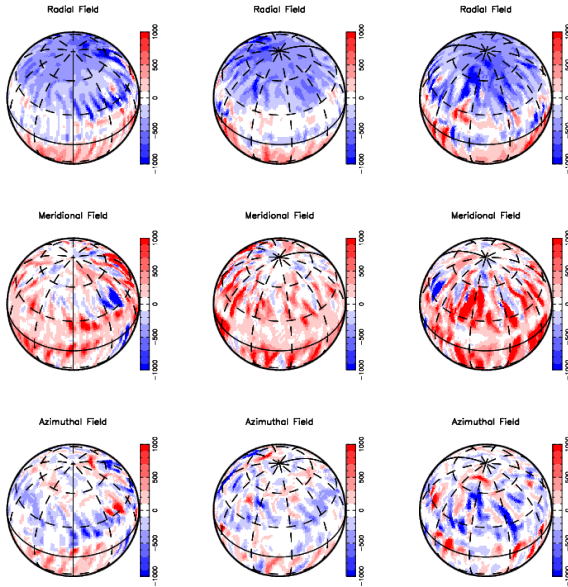
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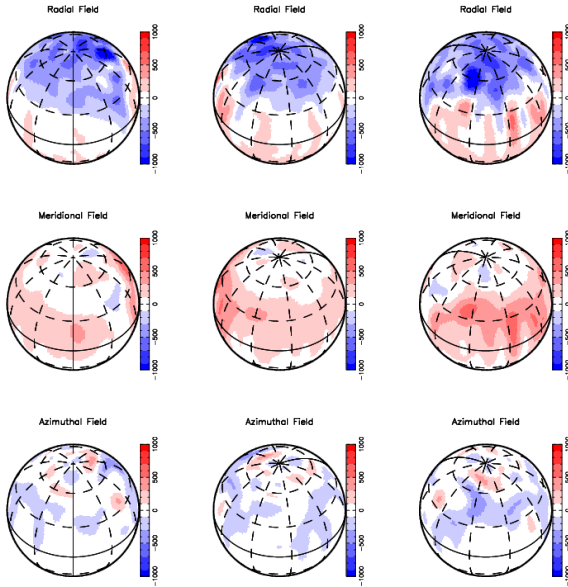
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ZDI: performances and limitations (1/2)



Input numerical simulation
Credit: T. Gastine
MagIC code

ZDI: performances and limitations (1/2)



ZDI reconstruction

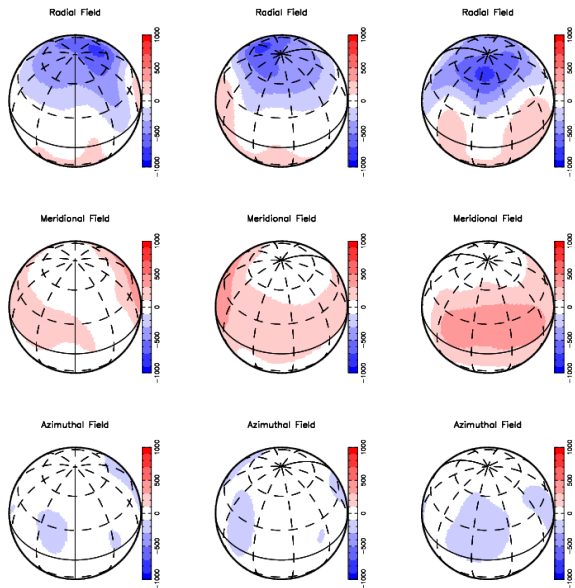
$v \sin i = 40 \text{ km/s}$

20 spectra

$S/N = 6,000$

$\ell_{\max} = 20$

ZDI: performances and limitations (1/2)



ZDI reconstruction

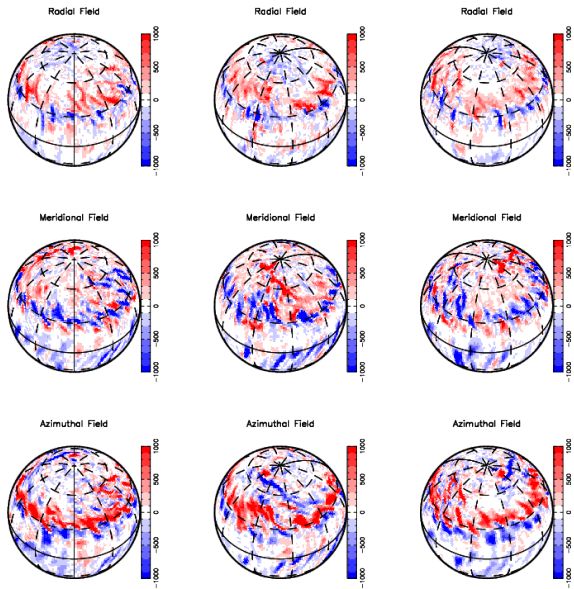
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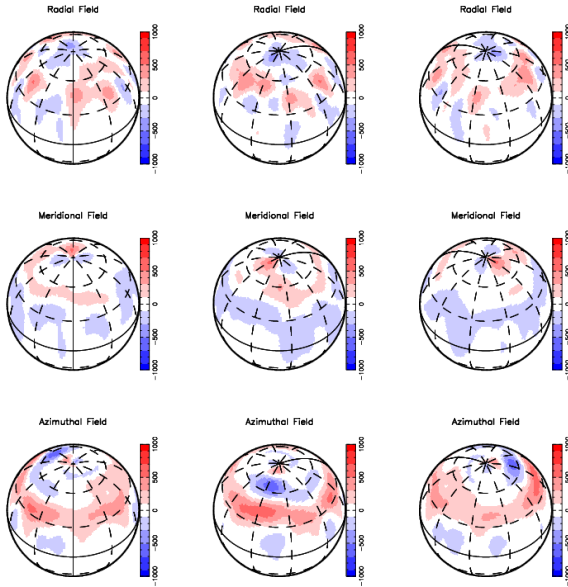


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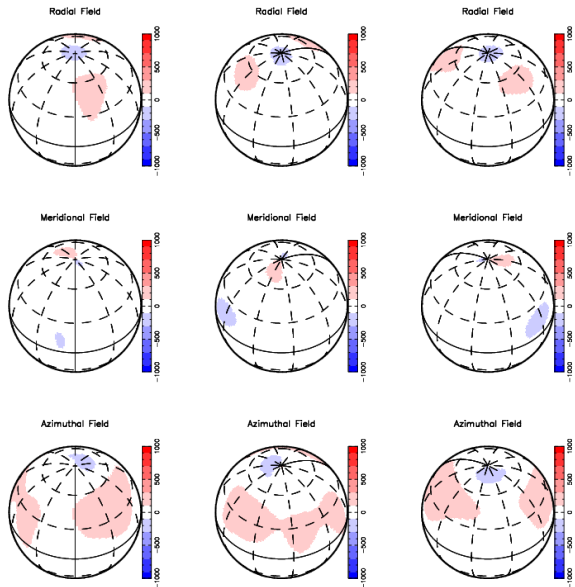
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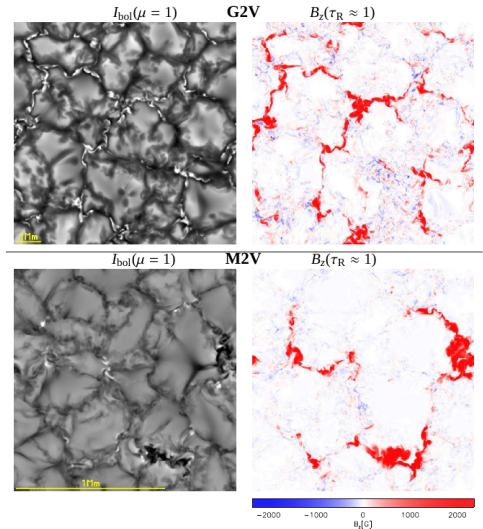
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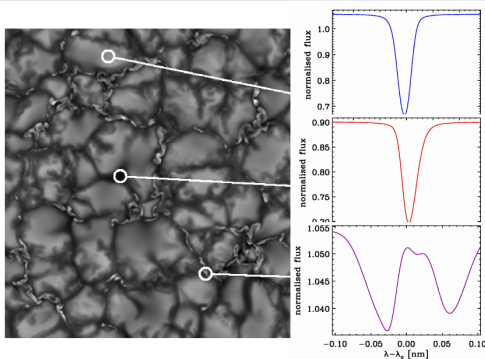
- Magnetic models assume
 - No velocity field
 - Homogeneous brightness
- How can we take them into account?



Beeck et al. (2011)

ZDI: performances and limitations (2/2)

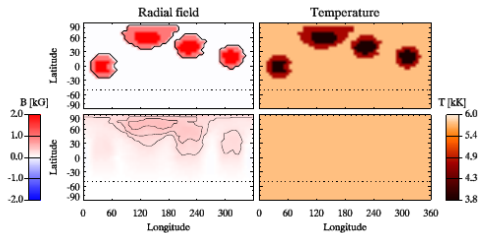
- Magnetic models assume
 - No velocity field
 - Homogeneous brightness
- How can we take them into account?



Credit: B. Beeck

ZDI: performances and limitations (2/2)

- Magnetic models assume
 - No velocity field
 - Homogeneous brightness
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Rosen & Kochukhov (2012)

Outline

- 1 Magnetic fields: a crucial ingredient of stellar physics
- 2 Detection and characterization of stellar magnetic fields
- 3 A (likely biased) selection of results
 - Chemically peculiar stars
 - Fully-convective stars
 - Young low-mass stars
 - And much more...
- 4 Summary

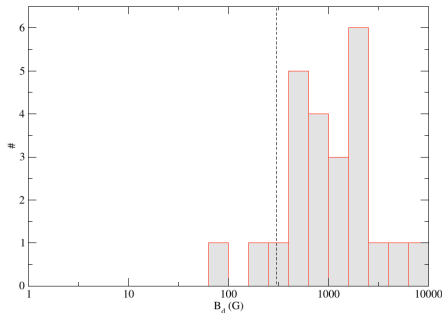
Chemically peculiar Ap/Bp stars

■ Detailed studies

- **B** can be more complex
- *Kochukhov & Wade (2010)*

■ *Aurière et al. (2007)*

- 100 % detection rate on Ap stars
- $B_{dip} > 300$ G
- Consistent w/ fossil scenario



Aurière et al. (2007)

Fully-convective stars

Dynamo action in FC stars

■ Solar dynamo

- Tachocline: crucial role?

■ Fully convective stars

- Tachocline $\rightarrow$ solar-dynamo

➡ observable effects?

■ Activity

■ B from Zeeman broadening

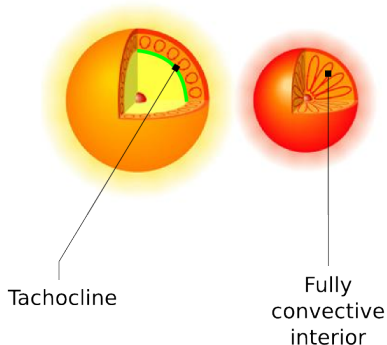
➡ No change at the fully-convective boundary

■ 1st spectropolarimetric survey

- Sharp transition $\sim 0.5 M_{\odot}$
- Multipolar $\rightarrow$ Dipolar B
- Significant $d\Omega \rightarrow \sim$ solid-body

Sun

Very low mass star



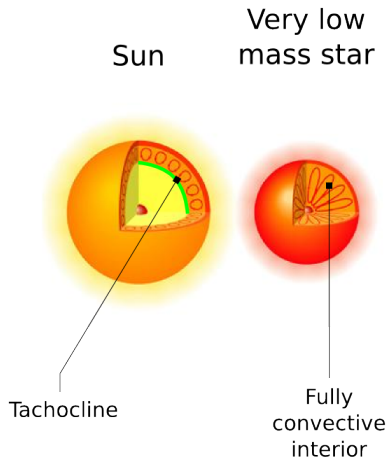
Internal structure of cool main sequence stars

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*Internal structure of cool
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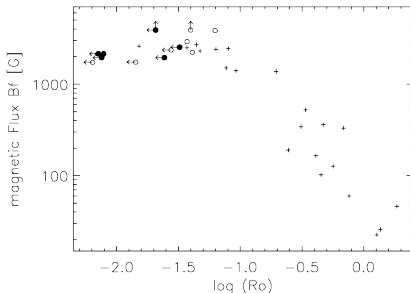
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Rotation-total magnetic field relation
Reiners, Basri & Browning et al. (2009)

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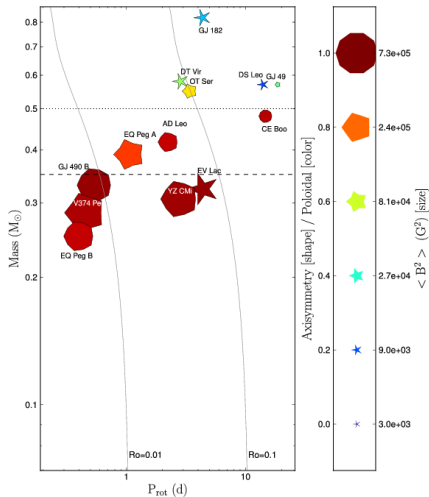
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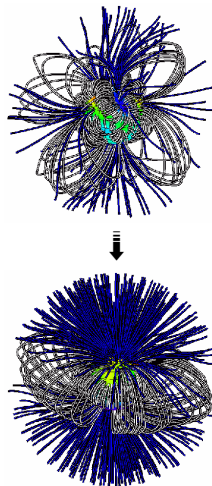


Donati et al. (2006, 2008), Morin et al. (2008a,b), Phan-Bao et al. (2009)

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Coronal extrapolations by M. Jardine from surface magnetic fields reconstructed by Donati et al. (2008), Morin et al. (2008)

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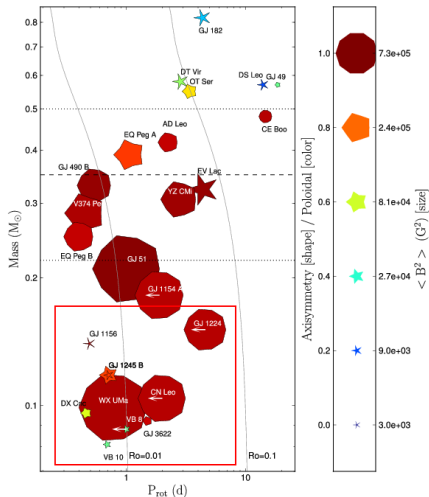
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Morin et al. (2010,2011)

Gastine et al. (2013)

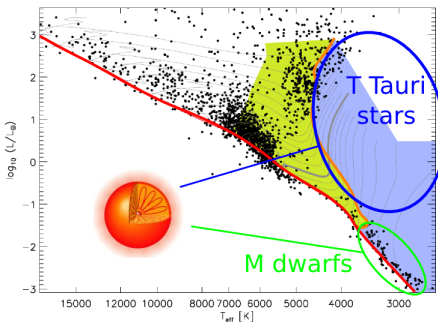
Young low-mass stars

■ T Tauri stars

- age 1 – 10 Myr
- Fossil or dynamo field?
- Field geometry?

■ MaPP LP CFHT

- Evolution on ~ 1 yr
- Dynamical evolution
- Variety properties
- Position in HRD
- Impulse new models



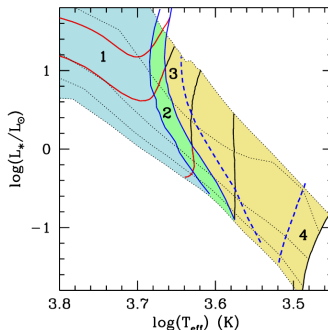
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Gregory et al. (2012)

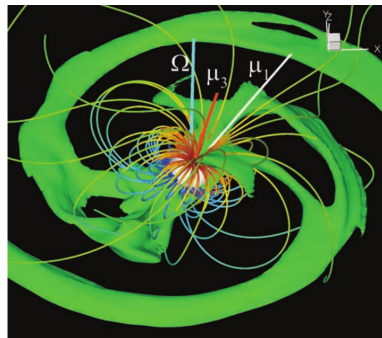
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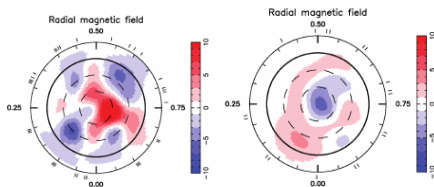
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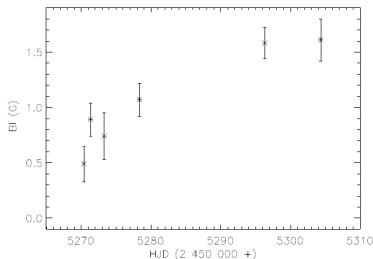
Romanova et al. (2011)

And much more...

- Solar twins
- Planet-host stars
- Intermediate mass stars
- Massive stars
- Evolved stars



Farès et al. (2009)



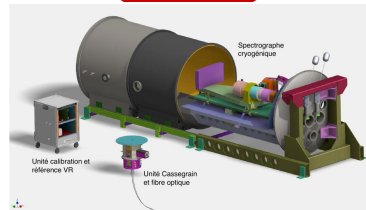
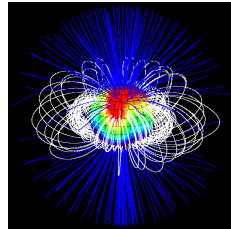
Aurière et al. (2010)

Outline

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Summary

- Magnetic fields
 - Crucial for stellar physics
 - Origin? Properties?
- Spectropolarimetry
 - Very high potential
 - Limitations to overcome
 - Important developments
- Important results
 - Across HRD
 - Detections
 - Physics
- Future
 - nIR spectropolarimetry
 - CFHT/SPIrou
 - CRIRES+



■ Stellar magnetism

- *Stellar Magnetism, Summer School on Stellar Physics XVII*
Eds. C. Neiner & J.-P. Zahn, 2009, EAS Publication Series, Vol. 39
- *Magnetic fields of non-degenerate stars*
J.-F Donati & J. Landstreet, 2009, ARAA, Vol. 47

■ Magnetism of cool stars

- *Observations of Cool-Star Magnetic Fields*
A. Reiners, 2012, Living Reviews in Solar Physics, Vol. 9
- *Magnetic Fields from Low-Mass Stars to Brown Dwarfs*
J. Morin, Eds. C. Reyl  , C. Charbonnel & M. Schultheis, 2012, EAS Publication Series, Vol. 57

■ Dynamo theory

- *The Magnetic Universe*
G. R  diger & R. Hollerbach, 2004, Wiley-VCH
- *Mathematical aspects of natural dynamos*
Eds. E. Dormy & A. Soward, 2007, CRC Press/Taylor & Francis